

Forecasting the New York State Economy with “Terraced” VARs and Coincident Indices

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ABSTRACT

This paper introduces “Terraced” Vector Autoregressive (VAR) models, an innovative twist on traditional VAR modeling, which allows the econometrician to simultaneously forecast both exogenous and endogenous variables and the confidence intervals around those forecasts.

In an application of our Terraced VAR framework, we have estimated coincident indices of economic activity for the United States, New York State and the six largest metropolitan areas of New York State and incorporated them into Terraced VARs, which forecast the unemployment rate, total non-farm employment, real wages and average hours worked in manufacturing in those regions.

I. Introduction

Forecasting regional economic variables poses a difficult task because the data series often exhibit negative first-order serial correlation (i.e. the series looks “jagged” or “saw-toothed”). Perhaps more importantly, the frequent fluctuations in the series make it difficult to discern whether a one-month increase in the unemployment rate or a one-month decrease in non-farm employment represent a deterioration of local economic conditions or simply represent the natural fluctuations of the series. Figures 1 and 2, which plot Rochester’s unemployment rate and non-farm employment level, illustrate the point.

To overcome this difficulty, we used Kalman’s (1960) filtering algorithm to estimate a coincident index of labor market activity from the unemployment rate, non-farm employment, average hours worked in manufacturing and real wages. Such an index of Rochester’s economy is shown in Figure 3.

Because the index does not exhibit negative first-order serial correlation, it follows a simple autoregressive process, which is relatively easy to forecast. And because the coincident index was estimated from the economic variables of interest to us, it is highly correlated with those variables and allows us to forecast them with more accuracy than we could achieve if we had not incorporated the coincident index into our forecasting models.

On a monthly basis, we use our forecasting model to produce reports on the state of New York’s labor market for the New York State Banking Department, which sponsored our research. Readers of

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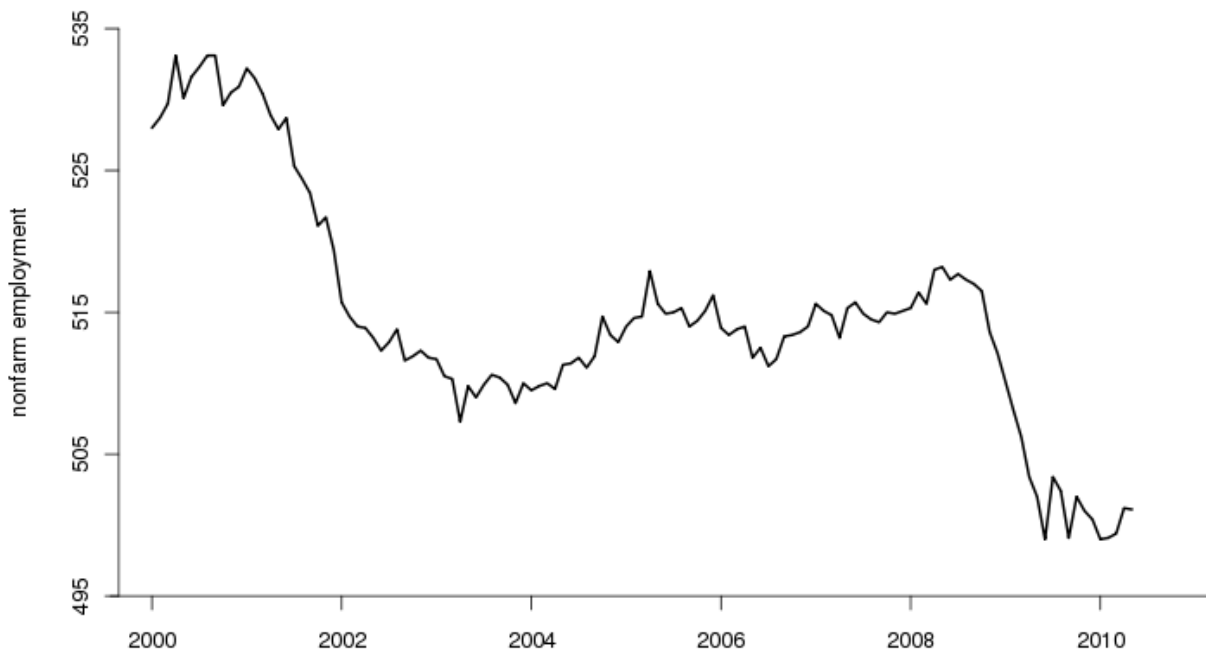
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Figure 1: Rochester Unemployment Rate (seasonally adjusted)



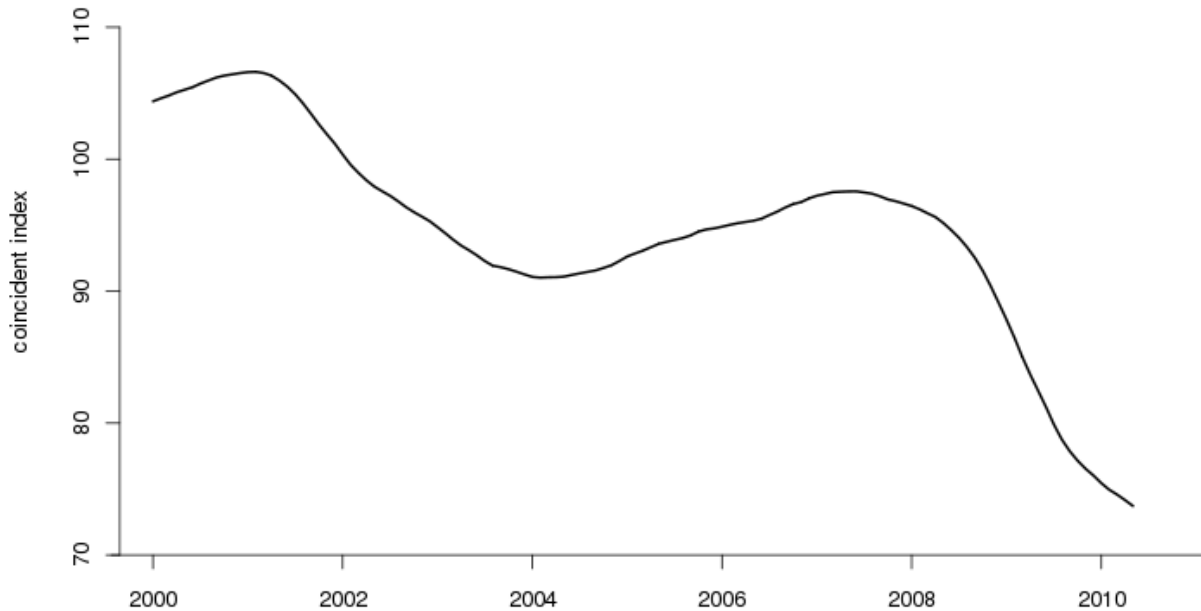
Note: The series depicted above ends in May 2010.

Figure 2: Rochester Nonfarm Employment (seasonally adjusted)



Note: The series depicted above ends in May 2010.

Figure 3: Coincident Index of the Rochester Economy



Note: The data used to generate the coincident index depicted above ends in May 2010.

the reports appreciate the visual smoothness of the coincident index because it allows them to quickly discern the trend in regional labor market activity.

Section II of this paper introduces and defines a methodology for constructing a coincident index of labor market indicators for the United States, New York State and the six largest metropolitan statistical areas (MSAs) of New York State¹. In explaining what a coincident index is, the paper also describes the coincident indices of national, state and regional economic activity that other economists have developed.

We did not develop coincident indices for their own sake. We developed them for the purpose of forecasting variables that depend on the state of the labor market, such as banks' non-current loans (a topic of particular interest to the Banking Department). To that end, we incorporated the coincident indices into "terraced" vector autoregressive (VAR) models, which can be used to forecast variables of interest, such as the unemployment rate and rates of foreclosure on residential mortgages.

In other words, we hypothesized that homeowners' difficulties in the labor market have been a major contributor to the recent increase in mortgage delinquency. We did find a strong correlation between our coincident indices and non-current loans, but we are reluctant to publish those findings because the FDIC's Statistics on Depository Institutions (our source of bank financial data) is only available on a quarterly basis since 2003 and on an annual basis since 1992.

The "terraced" VAR methodology, which we describe in section III, is our primary contribution to the economic literature. Unlike traditional VAR forecasting, "terraced" VARs do not require exogenous and endogenous variables to be forecast in two separate steps. Instead, the exogenous and

endogenous variables are forecast simultaneously, which allows the econometrician to obtain confidence intervals that depend only on the respective “predictor” variables.

For example, suppose that the New York City coincident index depends on past values of the national coincident index, but the reverse is not true. In such a simple, two-variable “terraced” VAR, the confidence interval around the forecast of the New York City index would depend on the residual variance of its regression equation, the residual variance of the national index’s regression equation and the covariance between them. By contrast, the confidence interval around the forecast of the national index would only depend on the residual variance of its own regression equation. Consequently, the “terraced” VAR methodology allows us to simultaneously compute the appropriate confidence intervals around both the New York City and national coincident indices.

Thus, the paper seeks to extend and build upon the existing literature on state-level coincident indices, while introducing new applications, such as incorporating the coincident indices into “terraced” VARs to forecast “key economic variables.” The indices can therefore help policymakers anticipate the future course of key economic trends. For example, the coincident indices can be used to forecast unemployment rates, total employment as well as indicators of banks’ financial health (e.g. rates of foreclosure filings and non-current loans). By including the forecast confidence intervals, we also provide policymakers with an indication of how accurate they can expect our forecasts to be. These uses of our methodology are briefly discussed in the conclusion of our paper, section IV.

II. Coincident Indices

1. Survey of Literature

In common speech, people often refer to the “state of the economy” with statements such as: “The economy is strong,” or “The economy is in bad shape right now.” As a question of measurement however, one must wonder what they are referring to. Are they referring to growth of real Gross Domestic Product (GDP)? Are they referring to growth of real household income? Are they referring to job growth? Are they referring to the unemployment rate?

Assuming that they are referring to some combination of those measures, how then do we evaluate a period in which real GDP grows, but the unemployment rate rises? Is the state of the economy “strong” or “weak?”

Obviously, one can easily define a weighted average of such measures, but what are the appropriate weights to apply to each measure? Should those weights be constant over time? Kacapyr’s (2010) Tompkins County index, for example, weights each element in inverse proportion to its volatility and adjusts the weights periodically. One can also imagine other reasons why the weights should not be constant over time. For example, if the economy is experiencing a structural shift, in which the manufacturing sector shrinks as the service sector grows, then it hardly makes sense to apply the same weight to manufacturing sector employment over time.

In addressing such questions, Stock and Watson (1989) made an original and valuable contribution to the econometric literature by observing that each of the measures described above depends on the underlying “state of the economy” and the particular characteristics that define each measure. They then used Kalman’s (1960) filtering algorithm to identify the unobservable “state of the economy” in a single index, called the “coincident index.”

Visually significant decreases in Stock and Watson’s original coincident index matched the beginnings and endings of recessions, as defined by the National Bureau of Economic Research (NBER). Visually significant increases, of course, corresponded to economic expansions. Stock and Watson also used a Vector Auto-Regression (VAR) model to forecast changes in the coincident index. The forecast of the coincident index is called the “leading index.”

More recently, two economists at the New York State Division of the Budget, Megna and Xu (2003), used Stock and Watson’s methodology to develop coincident and leading indices for the New York State economy, which they then used to forecast changes in state tax revenue.

There is major difference between Stock and Watson’s index and Megna and Xu’s index however. Specifically, Stock and Watson were interested in developing an index based on co-movements in several macroeconomic time series, whereas Megna and Xu were interested in forecasting state tax revenue. Consequently, they used different data series to develop their indices.²

Economists at the Federal Reserve Bank of New York have also developed a coincident index of the New York State economy. Orr et al. (1999) developed such an index to predict changes in the regional economy that do not necessarily coincide with national trends.³

A recent update of their index conducted by Bram et al. (2009) suggests that the New York regional economy remained far more resilient than the national economy (in the sense that the New York region entered the current recession several months later than the nation as a whole). They also found that New York State’s economic activity peaked in February 2008, while New York City’s continued to expand through June 2008. They also note that New York City’s economy has already experienced a “steeper downturn than a number of metropolitan areas in upstate New York.”

Such trends also appear in our own indices. Our indices suggest that the United States entered the current economic recession almost one year before the economies of New York State and New York City. Specifically, our indices date the national recession as beginning in March 2007, while New York State and New York City entered recession in May 2008 and March 2008 respectively.

More broadly, Crone and Clayton-Matthews (2005) applied Stock and Watson’s methodology to estimate a consistent set of coincident indicators for all 50 states. They developed their indices because the considerable lag with which the Bureau of Economic Analysis releases Gross State Product (GSP) series inhibits timely monitoring of state economic trends. In developing their index, they also found that the indices are a useful for comparing “the length, depth, and timing of recessions at the state level.”

The Federal Reserve Bank of Philadelphia (2009) argues that Crone and Clayton-Matthews' state coincident indices are comparable across states because they are generated from a consistent set of models and variables, but we remain skeptical. Specifically, we suspect that some of the indices may appear more volatile than others because the parameter values in their filters differ across states.

Even if they are correct however, the fact that there is less data available to us at the sub-state level than at the national and state level would prevent us from constructing an index of regional economic activity that is comparable to a state or national index unless we were willing to discard valuable data.

Consequently, the index that we develop for one region is not directly comparable to another's because the coincident indices do not have a common unit of measurement. New York City's index is measured in "New York City coincident units," while Rochester's index is measured in "Rochester coincident units."

2. Data Used to Estimate the Coincident Index

With two exceptions, the data that we used to estimate the coincident index were the same four data series that Crone and Clayton-Matthews (2005) used to develop coincident indices for all 50 states. Three of the four series that Crone and Clayton-Matthews used – nonagricultural payroll employment, the unemployment rate and average hours worked in manufacturing – are monthly data series from the US Bureau of Labor Statistics.

Although the unemployment rate is generally identified as a lagging indicator of economic activity, it is an appropriate variable to use when estimating the *current* state of the labor market. Moreover, its use as a coincident indicator of economic activity is consistent with the models established in the earlier works of Stock and Watson (1989), Orr et al. (1999), Megna and Xu (2003), and Crone and Clayton-Matthews (2005).

Because the fourth series that Crone and Clayton-Matthews used, the U.S. Bureau of Economic Analysis' quarterly real wages and salary disbursements series, is not available at the sub-state level, we calculated real wages by adjusting the U.S. Bureau of Labor Statistics' total wage series for inflation with the U.S. consumer price index. For consistency, we also used the total wage series in our estimates of the U.S. and New York State coincident indices.

The fact that the total wage series is quarterly, while the other series are monthly, does not pose a problem. In their paper, Crone and Clayton-Matthews show that interpolation is not necessary to handle mixed monthly and quarterly series. Instead, they show that the Kalman Filter can be adapted to handle any missing data simply by altering the dimensions of the relevant matrices. In fact, Petris' (2009) "dlm" package for R (R Development Core Team, 2008), which we used to implement the Kalman Filter, is designed to handle missing data.

In a second departure from Crone and Clayton-Matthews' framework, we did not use average hours worked in manufacturing in our sub-state coincident indices because the series is not available

at the sub-state level. We also did not use the real wage series in our estimates of the Rochester and Buffalo-Niagara Falls coincident indices because the extreme volatility of those series inhibited our ability to estimate the parameters of the Kalman Filter when we tried to include them.

Additionally, we used the US Census Bureau's X-12-ARIMA seasonal adjustment software (2007) to seasonally adjust the New York State "average hours" series, all of the quarterly wage series and the sub-state unemployment rates.

Finally, to account for serial correlation in the data series, we took differences of the unemployment rate series and log differences of the other series. Differencing also enabled us to overcome the problems associated with the change in industrial classification from SIC to NAICS, which was implemented by the U.S. Bureau of Labor Statistics in 1990. Since both classifications attempted to measure the same economic variable, we assumed that the log-differences of the two classifications are highly correlated with each other and switched from SIC to NAICS at the earliest possible point (i.e. from 1990 onward).

3. Estimation of the Coincident Index

To implement the Kalman Filter, we used a structure based loosely on the one used by Megna and Xu (2003)⁴. Specifically, we used the following structure for the measurement equation:

$$\begin{bmatrix} \Delta unemp_t \\ \Delta \ln(emp)_t \\ \Delta \ln(wages)_t \\ \Delta \ln(hours)_t \end{bmatrix} = \begin{bmatrix} \alpha_0 & \alpha_1 & \alpha_2 & \alpha_3 \\ \beta_0 & \beta_1 & 0 & 0 \\ \gamma_0 & \gamma_1 & \gamma_2 & 0 \\ \delta_0 & \delta_1 & 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta c_t \\ \Delta c_{t-1} \\ \Delta c_{t-2} \\ \Delta c_{t-3} \end{bmatrix} + \begin{bmatrix} u_{unemp,t} \\ u_{emp,t} \\ u_{wages,t} \\ u_{hours,t} \end{bmatrix} \quad (1)$$

and the following structure for the transition equation:

$$\begin{bmatrix} \Delta c_t \\ \Delta c_{t-1} \\ \Delta c_{t-2} \\ \Delta c_{t-3} \end{bmatrix} = \begin{bmatrix} \phi_0 & \phi_1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \Delta c_{t-1} \\ \Delta c_{t-2} \\ \Delta c_{t-3} \\ \Delta c_{t-4} \end{bmatrix} + \begin{bmatrix} v_t \\ 0 \\ 0 \\ 0 \end{bmatrix}, \quad (2)$$

where Δc_t is the change in the coincident index at time t and the residuals $u_{i,t}$ and v_t are assumed to have zero mean and constant variance.

As mentioned in section II.2, average hours worked in manufacturing is not available at the sub-state level, so the last row of equation 1 does not appear in the local economies' measurement equations.

We also used a slightly different structure for the measurement and transition equations of the Rochester and Buffalo-Niagara Falls Metropolitan Statistical Areas (MSAs). As mentioned in section II.2, we did not use the real wage series in our estimates of their coincident indices. We also found that a different structure worked better for their economies. Specifically, with the data for the Rochester

and Buffalo-Niagara Falls MSAs we used the following structure for the measurement equation:

$$\begin{bmatrix} \Delta unemp_t \\ \Delta \ln(emp)_t \end{bmatrix} = \begin{bmatrix} \alpha_0 & \alpha_1 & \alpha_2 & \alpha_3 \\ \beta_0 & \beta_1 & \beta_2 & 0 \end{bmatrix} \begin{bmatrix} \Delta C_t \\ \Delta C_{t-1} \\ \Delta C_{t-2} \\ \Delta C_{t-3} \end{bmatrix} + \begin{bmatrix} u_{unemp,t} \\ u_{emp,t} \end{bmatrix} \quad (3)$$

and the following structure for the transition equation:

$$\begin{bmatrix} \Delta C_t \\ \Delta C_{t-1} \\ \Delta C_{t-2} \\ \Delta C_{t-3} \end{bmatrix} = \begin{bmatrix} \phi_0 & \phi_1 & \phi_2 & \phi_3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \Delta C_{t-1} \\ \Delta C_{t-2} \\ \Delta C_{t-3} \\ \Delta C_{t-4} \end{bmatrix} + \begin{bmatrix} v_t \\ 0 \\ 0 \\ 0 \end{bmatrix}. \quad (4)$$

Although the transition equations are designed to yield a single index, Petris’ (2009) “dlm” package, which we used to implement the Kalman Filter, does not output a single index. Instead, it outputs four (one for each row of the transition equation). In practice however, each successive index contains the lagged values of the previous one and (after accounting for the lags) the differences between the four indices can safely be ignored.

4. What the Coincident Index Tells Us

To evaluate the quality of our coincident indices, it is helpful to compare our national and New York State index with the national and New York State indices published by the Federal Reserve Bank of Philadelphia and with Megna and Xu’s (2003) New York State index. Figures 4 and 5 provide a visual comparison of our indices with those published by the Philadelphia Fed and the text of this section provides a qualitative comparison.⁵

As mentioned in Section II.1, visually significant decreases in the coincident index indicate that the economy is in recession. Consequently, the peaks and troughs in the index can be used to mark the beginnings and endings of economic recessions. Therefore, the periods during which our coincident index indicates that the economy was in recession should roughly correspond to the recessionary periods in their indices.

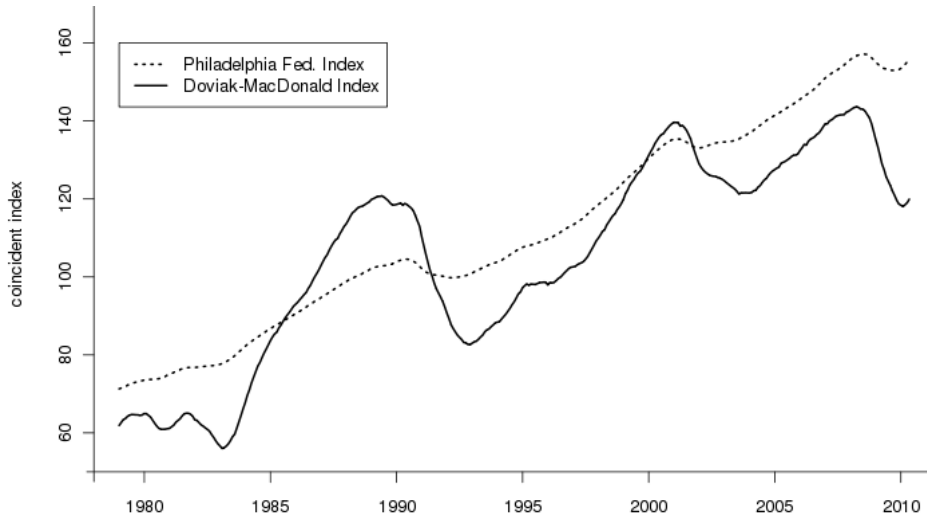
As Figures 4 and 5 show, our indices exhibit much more dramatic swings in labor market activity than the Philadelphia Fed’s indices do. This difference does not bother us. On the contrary, we feel that the dramatic swings in our indices more accurately reflect the state of the labor market.

For example, the value of the Philadelphia Fed’s index for the US economy was 158.55 in May 2010, which was roughly the same as the 158.66 reading in February 2006. The state of the labor market was very different at those two points in time however. After all, the unemployment rate was 4.9 percentage points higher and non-farm employment was 3.5 percent lower in May 2010 than it

was in February 2006. By contrast, our United States index value was 107.0 in February 2006 and 52.5 in May 2010.

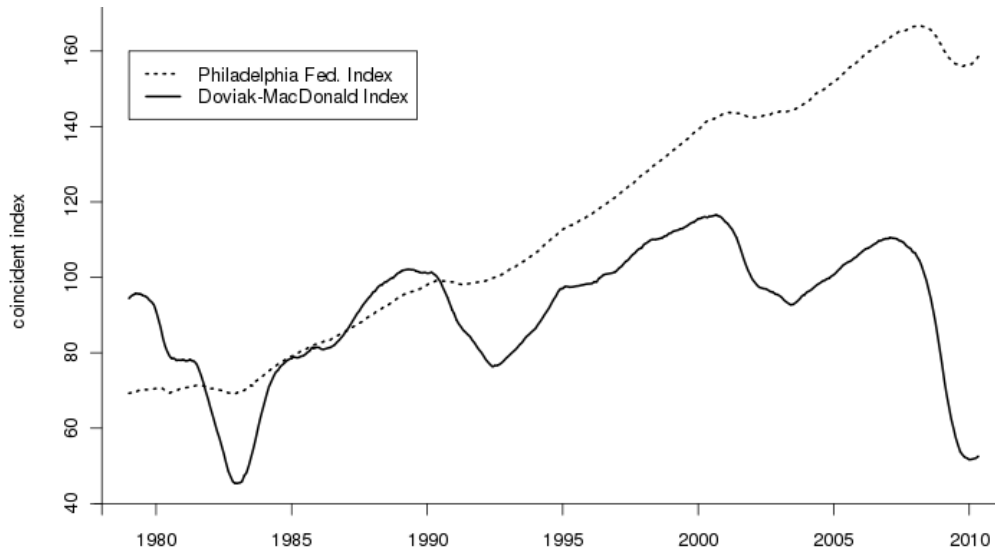
Similarly, the value of the Philadelphia Fed's index for the New York State economy was 155.32 in May 2010, which was roughly the same as the 155.32 reading in December 2007. Once again, the state of the labor market was very different in those two periods. New York's unemployment rate was 3.6 percentage points higher and its non-farm employment was 2.5 percent lower in May 2010 than it was in December 2007. Once again, our New York index more accurately reflects the change in the state of the labor market, as its index values were 142.5 in December 2007 and 119.9 in May 2010.

Figure 4: Coincident Indices of the New York State Economy



Note: The series depicted above ends in May 2010.

Figure 5: Coincident Indices of the United States Economy



Note: The series depicted above ends in May 2010.

More broadly, the Philadelphia Fed's indices do not account for the “jobless” recoveries that characterized the previous two recessions. By contrast, our indices exhibited longer periods of recession than the Philadelphia Fed's indices did, which suggests that our indices account for the structural changes that occurred in the US and New York State labor markets. The Philadelphia Fed's indices do not. In particular, our indices capture the effect that the manufacturing sector's decline has had on upstate labor markets since it began shrinking in 1990.

This effect of the manufacturing sector's decline is strikingly evident in our Rochester index which peaked in 2001 and never recovered from the subsequent recession (as can be seen in Figure 3).

Figure 4 provides a graphical comparison of our New York State index to the one developed by the Philadelphia Fed and illustrates the tendency of our index to show longer periods of recession. For example, our index indicates that the New York State economy entered a recession in October 1979 and did not recover until November 1980. By contrast, the Philadelphia Fed index indicates that that recession began in March 1980 and ended in July 1980, a mere four months in comparison with our 13 months. We were unable to obtain the data necessary to plot Megna and Xu's New York State index, but their paper states that the recession ran from March 1980 to September 1980.

All three New York State indices indicate that the next New York State recession began in September 1981, but our index and Megna and Xu's index indicate that it ended in February 1983, while the Philadelphia Fed index indicates that it ended three months earlier, in November 1982.

At the end of the 1980s, both our index and the Philadelphia Fed index suggest that New York State's economy plateaued for over a year before entering recession in the second quarter of 1990, but our index indicates that the recession lasted longer than the Philadelphia Fed index does. Specifically, our index indicates that it ended in September 1992, whereas the Philadelphia Fed index indicates that it ended in June 1992. By contrast, Megna and Xu's index shows a peak in June 1989 and a long recession that didn't end until November 1992.

Our index and the Philadelphia Fed index also show a common beginning to the New York State recession that began in February 2001, but once again our index indicates that it lasted longer than the Philadelphia Fed index does. Specifically, their index indicates that it ended in March 2003, while our index indicates that it ended in August 2003.

Figure 5 shows sharp differences between our index and the Philadelphia Fed's regarding when the U.S. economy enters recession and how long it lasts. Generally speaking, our index suggests earlier beginnings and longer durations of economic recessions than theirs. For example, our index indicates that the United States entered the current economic recession in March 2007, whereas the Philadelphia Fed index indicates that the national economic recession began in April 2008.

Similar discrepancies are also seen in the dating of other recessions as well. At the extreme, our index indicates that the previous national recession began in October 2000 and lasted 33 months, while the Philadelphia Fed index places its beginning at June 2001 and indicates that it lasted only eight months.

A similarly large difference exists in the dating of the national recession of the early 1990s. Our index indicates that it lasted from April 1990 to June 1992, whereas the Philadelphia Fed indicates that it lasted from October 1990 to May 1991.

The differences in the dating are smaller however when we compare the dating of the two recessions in the early 1980s. Our index indicates that the first one began in July 1979 and lasted 14 months, while the Philadelphia Fed index indicates that the first one began in April 1980 and lasted four months. There is slightly more agreement on the dating of the second recession in the early 1980s. Our index indicates that it lasted from May 1981 until January 1983, whereas the Philadelphia Fed index indicates that it lasted from September 1981 until November 1982.

These few similarities aside, our indices and the Philadelphia Fed's disagree sharply on the dates when recessions began and ended (because our indices suggest that recessions last longer). On a very general level however, their indices and ours both identify the same recessions. If the Philadelphia Fed's indices are considered a benchmark, then this rough similarity in dating would still allow us to conclude that our indices adequately capture movement in overall economic activity in both the United States and New York State.

III. Forecasting

Because the coincident index measures the underlying state of the labor market, forecasts of the coincident index (called a "leading index") predict the future course of labor market activity and provide policymakers with an outlook for the future course of variables that depend on the state of the labor market, such as banks' non-current loans and rates of mortgage delinquency.

Because it is constructed from the unemployment rate, non-farm employment and average hours worked in manufacturing, the coincident index is also an excellent predictor of those variables, so we include forecasts of these "key economic variables" in our monthly reports. These forecasts have the added benefit of providing the reader of our reports with a concrete understanding of what the coincident index forecast means.

1. "Terraced" VARs

Our forecasting model consists of a set of "terraces." The top terrace forecasts exogenous variables that are useful in predicting changes in the national coincident index. The forecasts of those exogenous variables are passed down to the next terrace, which forecasts the change in the national coincident index. The national index forecast is then passed down to the next terrace, which forecasts the change in a sub-national index. Finally, at the lowest level, the sub-national index forecast is used to forecast changes in the "key economic variables."

Forecasts on a given terrace are based on autoregressive models, which assume that the change in a given variable depends on past changes in that variable and on past changes in variables at higher level terraces. To be more concrete, this section will explain our forecasting model in terms of a

simple three variable “terraced” vector autoregressive (VAR) model. In practice, there are many more variables in our model, but – to keep the example simple here – these will be discussed in further detail in Section III.4.

The specific example of a terraced VAR that we will use is as follows:

$$\begin{bmatrix} \Delta US_t \\ \Delta NYC_t \\ \Delta unemp_t \end{bmatrix} = \begin{bmatrix} \alpha_{US} & 0 & 0 \\ \beta_{US} & \beta_{NYC} & 0 \\ 0 & \gamma_{NYC} & \gamma_{unemp} \end{bmatrix} \begin{bmatrix} \Delta US_{t-1} \\ \Delta NYC_{t-1} \\ \Delta unemp_{t-1} \end{bmatrix} + \begin{bmatrix} u_{US,t} \\ u_{NYC,t} \\ u_{unemp,t} \end{bmatrix}. \quad (5)$$

The top row of equation 5 (or “top terrace”) models the change in the U.S. coincident index at time t (denoted: ΔUS_t). In this case, it is assumed that ΔUS_t depends only on the previous value of the change in the US index (i.e. ΔUS_{t-1}) and the residual: $u_{US,t}$. In such a model, forecasts of the change in the U.S. coincident index will therefore depend exclusively on past values of the change in the US index.

The second row models the change in the New York City coincident index at time t (denoted: ΔNYC_t). According to equation 5, ΔNYC_t depends on ΔUS_{t-1} , its own past value (i.e. ΔNYC_{t-1}) and the residual: $u_{NYC,t}$. Forecasts of the change in the New York City coincident index will therefore depend on past values of the change in the New York City index as well as past values of the change in the U.S. index.

Finally, the third row models the change in the New York City unemployment rate at time t (denoted: $\Delta unemp_t$). In this case, it is assumed that $\Delta unemp_t$ depends on ΔNYC_{t-1} , its own past value (i.e. $\Delta unemp_{t-1}$) and the residual: $u_{unemp,t}$. Forecasts of the change in the New York City unemployment rate will depend on past values of the change in the New York City unemployment rate and past values of the change in the New York City coincident index. It is important to note that forecasts of the change in the New York City unemployment rate will also depend on past values of the change in the U.S. index (because the change in the New York City index depends on past values of the change in the U.S. index).

To set up the terraced VAR, we first created an ordinary VAR using Pfaff’s (2008) “vars” package for R (R Development Core Team, 2008). We then used ordinary least squares (OLS) regression to estimate the coefficients of the terraced VAR and replaced the ordinary VAR coefficients with the coefficients of the terraced VAR.

We also replaced the residuals in the VAR object with the rescaled residuals⁶ from the OLS equations, so that the VAR object’s residual covariance matrix could be used to compute the confidence intervals around our forecasts.

2. Long-Run Assumptions

As mentioned previously, a terraced VAR models *changes* in the variables of interest. We had to express each model in terms of changes to remove the spurious correlation that arises between two unrelated variables that trend upward (or downward) over time.

We also had to make sure that our terraced VARs do not contain a “unit root,” so that the effect of any given shock will fade over time. (In other words, the model assumes that the events of 20 or 30 years ago do not affect the month-to-month fluctuations in the variables we are examining.)

Because all shocks fade over time and because our terraced VARs do not contain an intercept term, our models implicitly assume that the changes in the coincident index and changes in the key economic variables converge to zero in the long run. Since the changes are zero in the long run, the model assumes that the coincident index and key economic variables remain constant in the long run.

In theory, this implies a prediction that the economy will never recover from the current economic crisis. In practice however, forecasts of exogenous leading economic indicators, such as unfilled orders for durable goods (discussed in Section III.4) act as an implicit intercept, which allow our model to predict both recovery from recession and decline from expansion.

3. Confidence Intervals

When forecasting, we must assume that the errors in equation 5 will equal zero. In other words, when forecasting the New York City coincident index we implicitly assume that we know the future course of the US index with certainty. Similarly, when we forecast the New York City unemployment rate we implicitly assume that we know the future course of the New York City index with certainty.

Of course, we do not know those values with certainty. All of our forecasts are prone to error, which we must account for. To that end, we estimate a range of forecast values, within which we can be 90 percent certain that the true values will fall. As mentioned in Section 3.1, these estimates are based on the residuals that we obtained when we estimated the coefficients of the terraced VAR.

To compute the confidence intervals, Pfaff’s “vars” package uses forecast error variance decomposition, which is based on the Wold (1954) moving average decomposition for stable VAR-processes, which is defined as:

$$\mathbf{y}_t = \Phi_0 \mathbf{u}_t + \Phi_1 \mathbf{u}_{t-1} + \Phi_2 \mathbf{u}_{t-2} + \dots, \quad (6)$$

where \mathbf{y}_t is the vector of dependent variables at time t , \mathbf{u}_{t-i} is the residual vector at time $t - i$ and the Φ_i are matrices of parameters that depend on the coefficients of the VAR (or terraced VAR in our case). If the residuals are interpreted as unforeseen economic shocks, then equation 6 shows that current changes in our model’s variables depend entirely on past shocks.

To compute the values of Φ_i , Pfaff’s “vars” package sets Φ_0 equal to an identity matrix (with the same number of dimensions as the VAR has variables) and recursively computes Φ_s as:

$$\Phi_s = \sum_{j=1}^s \Phi_{s-j} A_j \quad \text{for } s = 1, 2, \dots, \quad (7)$$

where A_j is matrix j of the p matrices of VAR coefficients⁶ and where $A_j = 0$ for $j > p$. The values of Φ_i

are then used to compute the forecast error covariance matrix:

$$\text{Cov} \left(\begin{bmatrix} \mathbf{y}_{T+1} - \mathbf{y}_{T+1|T} \\ \vdots \\ \mathbf{y}_{T+h} - \mathbf{y}_{T+h|T} \end{bmatrix} \right) = \begin{bmatrix} I & 0 & \dots & 0 \\ \Phi_1 & I & & 0 \\ \vdots & & \ddots & 0 \\ \Phi_{h-1} & \Phi_{h-2} & \dots & I \end{bmatrix} (\Sigma_u \otimes I_h) \begin{bmatrix} I & \Phi_1^T & \dots & \Phi_{h-1}^T \\ 0 & I & & \Phi_{h-2}^T \\ \vdots & & \ddots & \vdots \\ 0 & 0 & 0 & I \end{bmatrix}, \quad (8)$$

where T is last period for which data is available, h is the number of forecast periods, I_h is an identity matrix with h dimensions, Σ_u is the residual covariance matrix, the operator \otimes is the Kronecker product and $\mathbf{y}_{T+h} - \mathbf{y}_{T+h|T}$ is the difference between the true value of the dependent variable vector at time $T+h$ and our forecast of it, given the information available to us at time T .

The square roots of the diagonal elements of the forecast error covariance matrix are the standard errors of the forecasted variables, which we then use to compute the confidence intervals.

Had we estimated the terraced VAR that was used as an example in Section III.1 and then computed the confidence interval around its forecasts, we would find that the confidence interval around the U.S. coincident index is computed as if the New York City variables were not in the terraced VAR at all.

The confidence interval around the New York City index would depend on the variances of the U.S. and New York City index residuals and the covariance between them (i.e. just as if it had come from a standard two-variable VAR), but would be blind to the presence of the New York City unemployment rate in the terraced VAR.

In the third forecast period (and thereafter), the confidence interval around New York City's unemployment rate would depend on all six variances and covariances (just as one would expect from the model).

There are two sources of error, however, that the forecast error variance decomposition cannot account for. One is revisions of the data used to generate the index and forecasts. The other is sampling error. Forecast error variance decomposition does not account for sampling error because it implicitly assumes that the VAR's coefficients are exactly equal to their true values. Had we estimated the coefficients from a different time interval, we would have obtained different coefficient estimates and thus gotten a different forecast.

As Feldstein (1971) has shown, sampling error implies that the forecast error of the New York City variables (in Section III.1) would not be distributed normally. To overcome the problems associated with non-normality, McCullough (1996) proposed bootstrapping.

We have chosen not to use bootstrapped confidence intervals however for two reasons. First, given the complexity of our models, the bootstrapping code is very difficult to write and could introduce an unknown degree of human error into the bootstrapped confidence intervals. Second, the purpose of this exercise is to provide the reader of our reports with a general sense of the direction in which the national, state and local economies are headed and with a basic sense of accuracy. We do not need precise estimates of the distribution of the forecast error.

4. Forecast Accuracy

It is simple to create a terraced VAR and compute the confidence intervals around its forecasts, but there are many possible terraced VAR structures to choose from. Therefore, we need to select the structure that has the most predicative power. In this section, we also wish to show that using coincident indices in our forecasting models increases the model's predicative power.

To that end, we estimated the coefficients of many possible terraced VAR structures using the available data between from 1990 to 2004. We then used the estimated coefficients and the rest of the available data (which ended in December 2008) to create 37 sets of 12-month forecasts and 11 sets of shorter forecasts. Finally, we compared the forecasts to the actual values and computed the Mean Squared Error (MSE) of the model's forecasts:

$$MSE_k = \frac{1}{n} \sum_{i=0}^{n-1} (y_{T+i+k} - y_{T+i+k|T+i})^2 ,$$

where k is the number of periods ahead for which the variable y_t is forecasted, $y_{T+i+k|T+i}$ is the forecasted value of y_{T+i+k} given the information available at time $T+i$ and n is the number of k -period ahead forecasts.

As Greene (2000) notes, the MSE does not have a scale which allows us to compare the MSE of one forecasted variable to the MSE of another. To get around this problem, we compared the MSE to the variance of the forecasted variable by creating a "relative MSE" statistic, which is similar in spirit to the coefficient of determination:

$$Rel.MSE_k = 1 - \frac{MSE_k}{var(y_{t+k})}$$

where $var(y_{t+k})$ is the variance of the variable y_{t+k} in the forecast period.

A relative MSE of one implies perfect prediction, while lower values imply weaker forecasting performance. It is important to note that this statistic may be negative, but – because we cannot know what the variable's mean will be in the forecast period – negativity does not necessarily mean that the forecast is poor. Sometimes, a slightly negative relative MSE is the highest value one can obtain when forecasting a very volatile variable.

Table 1 uses relative MSE to compare our forecast models to both a random walk and an "alternative model," in which the region's coincident index is not used to forecast "key economic variables" (i.e. the unemployment rate, non-farm employment and average hours worked in manufacturing). To keep the table concise, the reported relative MSE statistic is the average of the 12 $Rel.MSE_k$:

$$Rel.MSE = \frac{1}{12} \sum_{k=1}^{12} Rel.MSE_k$$

Table 1 shows that our forecast models always outperform the “random walk” forecasts (i.e. $y_{T+k|T} = y_T$ for all k). In other words, our forecast models always provide better prediction than simply observing present economic conditions and assuming that the same condition will continue to hold for the foreseeable future.

With three exceptions, Table 1 shows that our forecast models always outperform the forecasts of the “alternative model,” which is the best model that we could develop that does not include the region’s coincident index as an explanatory variable. This shows that the region’s coincident index is a good predictor of the variables that were used to create it.

The three exceptions were the unemployment rates of New York State and the Nassau-Suffolk MSA and non-farm employment of the Putnam-Rockland-Westchester MSA, but in each of these cases, the difference between the forecast model and the alternative model was small. Given the proximity of Nassau-Suffolk and Putnam-Rockland-Westchester to New York City, it may be the case that the labor markets in these two MSAs are more dependent on the state of the New York City economy than they are on their own. Moreover, the fact that New York City accounts for approximately 43 percent of the New York State population, the New York State unemployment rate may also be heavily dependent on the state of the New York City economy.

Interestingly, the coincident indices turned out to be good predictors of themselves. This may be attributable to the auto-regressive processes that the coincident indices follow (i.e. to the “smoothness” of the coincident index series).

The U.S. coincident index also appears to be a good predictor of state and regional coincident indices. This may be attributable to the fact that regional economies are strongly influenced by national economic conditions.

While developing our forecasting models, we also experimented with other variables, such as the Federal Reserve’s measures of industrial production and capacity, the Census Bureau’s series on housing starts, durable goods and retail sales. The model that provided the most predicative power however only included the Census Bureau’s durable goods unfilled orders series as an exogenous variable.

Housing starts, which are often mentioned as a leading indicator, did not prove to be a good predictor of our indices. The lack of correlation may be attributable to the fact that the time period over which we tested our forecast models includes the period during which the housing bubbles in the U.S. and New York State burst. Housing starts were very weak from January 2007 through mid-2009.

In any case, forecast models that included unfilled orders for durable goods proved to be a significantly stronger predictor of our indices than forecast models that included housing starts.

Taken as a whole, one can conclude from the reasonably high values of our forecast models’ relative MSE statistics that our forecasting models capture a good share of the out-of-sample variation in the variables that the models predict.

Table 1: Forecast Accuracy

	<i>Forecast Model</i>		Alternative Model		R. Walk
	Rel. MSE	specification	Rel. MSE	specification	Rel. MSE
United States					
Dur. Goods Unfill. Orders	-0.220	DGU(1,2,3,4,5,6)			-0.770
Coincident Index	0.609	DGU(4), US(1,2)			0.494
Unemployment Rate	0.348	US(1,2), UR(1,2)	-0.020	DGU(4), UR(1,2)	-0.320
Nonfarm Employment	0.615	US(1,2), EMP(1,2)	0.390	DGU(4), EMP(1,2)	0.273
Avg. Hours Worked Manuf.	0.080	US(1,2), HR(1,2)	0.001	DGU(4), HR(1,2)	-0.752
New York State					
Coincident Index	0.475	US(1,2), NYS(1,2), NYC(1,2)			0.069
Unemployment Rate	0.368	US(1,2), NYS(1,2), UR(1,2)	0.371	US(1,2), NYC(1,2), UR(1,2)	-0.449
Nonfarm Employment	0.185	NYS(1,2), EMP(1,2)	-0.045	US(1,2), NYC(1,2), EMP(1,2)	-0.640
Avg. Hours Worked Manuf.	0.047	US(1,2), NYS(1,2), NYC(1,2), HR(1,2)	0.028	US(1,2), NYC(1,2), HR(1,2)	-0.895
New York City					
Coincident Index	0.783	US(1,2), NYC(1,2)			0.408
Unemployment Rate	0.259	US(1,2), NYC(1,2), UR(1,2)	0.241	US(1,2), UR(1,2)	-0.703
Nonfarm Employment	0.147	NYC(1,2), EMP(1,2)	-0.234	US(1,2), EMP(1,2)	-0.468
Nassau-Suffolk					
Coincident Index	0.773	US(1,2), NYC(1,2), NS(1,2)			0.419
Unemployment Rate	0.263	US(1,2), NYC(1,2), NS(1,2), UR(1,2)	0.269	US(1,2), NYC(1,2), UR(1,2)	-0.509
Nonfarm Employment	0.166	NYC(1,2), NS(1,2), EMP(1,2)	0.134	US(1,2), NYC(1,2), EMP(1,2)	-0.740
Putnam-R'land-West'r					
Coincident Index	0.661	US(1,2), NYC(1,2), PRW(1,2)			0.479
Unemployment Rate	0.229	PRW(1,2), UR(1,2)	0.216	US(1,2), NYC(1,2), UR(1,2)	-0.537
Nonfarm Employment	0.058	US(1,2), NYC(1,2), PRW(1,2), EMP(1,2)	0.095	US(1,2), NYC(1,2), EMP(1,2)	-1.030

Table continues on the next page

Table 1 (continued): Forecast Accuracy

	Forecast Model		Alternative Model		R. Walk
	Rel. MSE	specification	Rel. MSE	specification	Rel. MSE
Buffalo-Niagara Falls					
Coincident Index	0.641	US(1,2), BN(1,2)			0.456
Unemployment Rate	0.254	US(1,2), BN(1,2), UR(1,2)	0.207	US(1,2), UR(1,2)	-0.721
Nonfarm Employment	0.031	BN(1,2), EMP(1,2)	-0.012	US(1,2), NYS(1,2), EMP(1,2)	-1.055
Rochester					
Coincident Index	0.660	US(1,2), Rch(1,2)			0.505
Unemployment Rate	0.292	US(1,2), NYS(1,2), Rch(1,2), UR(1,2)	0.240	US(1,2), NYS(1,2), UR(1,2)	-0.603
Nonfarm Employment	-0.039	NYS(1,2), Rch(1,2), EMP(1,2)	-0.210	US(1,2), EMP(1,2)	-1.168
Albany-Sch.-Troy					
Coincident Index	0.721	US(1,2), NYS(1,2), AST(1,2)			0.496
Unemployment Rate	0.193	US(1,2), NYS(1,2), AST(1,2), UR(1,2)	0.169	US(1,2), NYS(1,2), UR(1,2)	-0.774
Nonfarm Employment	0.124	AST(1,2), EMP(1,2)	0.122	US(1,2), NYS(1,2), EMP(1,2)	-1.030

The numbers in parenthesis are the lag numbers of the variables that appear in the model's equation.

DGU – Durable Goods Unfilled Orders
 US – United States Coincident Index
 NYS – New York State Coincident Index
 NYC – New York City Coincident Index
 NS – Nassau-Suffolk Coincident Index
 PRW – Putnam-Rockland-Westchester Coincident Index

BN – Buffalo-Niagara Falls Coincident Index
 Rch – Rochester Coincident Index
 AST – Albany-Schenectady-Troy Coincident Index
 UR – Unemployment Rate
 HR – Average Hours Worked in Manufacturing
 EMP – Nonfarm Employment

IV. Conclusion and Direction for Future Research

This paper has explained what a coincident index is and has detailed the methodology employed to estimate the values of the coincident index for the United States, New York State and the six largest MSAs in New York State. It has also explained how we use the coincident index to forecast the future course of “key economic variables” in those regions.

No forecast will ever be perfect; however, we account for the inevitable error in our forecasts by using Terraced VARs to simultaneously forecast all of the variables in the model and compute confidence intervals that depend solely on the variables that affect the value of the forecasted variables. The confidence intervals are imperfect because they do not account for sampling error, but these imperfections occur in all VAR model forecast confidence intervals (not just terraced VARs).

As Section III.4 has shown, our forecasts are more accurate than those we could obtain from assuming a random walk and those that we would obtain had we not included the coincident index in our forecasting models.

In future work, we will explore the correlation between our index and other variables of interest. For example, to the extent that borrowers’ ability to meet their monthly mortgage and consumer credit payments depends on the state of their local economy, then we can examine whether there is a correlation between loans past due and the coincident index. We have already found such a correlation in our preliminary work, so we hope to use the forecast of the coincident index to forecast loans past due and predict future delinquency trends.

ENDNOTES

1. The coincident index estimates exclude Utica-Rome, Syracuse, Elmira, and Binghamton due to insufficient data.
2. Stock and Watson used data on industrial production, personal income net of transfer payments, hours worked by employees of nonagricultural establishments and total manufacturing and trade sales to develop their index, while Megna and Xu used data on total employment, sales tax revenue (as a proxy for retail sales), hours worked in manufacturing and the unemployment rate.
3. Orr et al. developed their index from data on total employment, real wages and salaries, the unemployment rate and average hours worked in manufacturing.
4. It should be noted, however, that Megna and Xu’s framework used monthly sales tax collection data as a proxy for retail sales instead of a real wage series.
5. We requested, but were unable to obtain, Megna and Xu’s New York State index. Our comparisons with their results are based on their published paper.
6. Rescaling the residuals was necessary to account for the difference in degrees of freedom between the ordinary VAR and the OLS regression.
7. The number of VAR coefficient matrices, p , is equal to the lag order of the VAR.

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